



GRAPH-THEORETIC APPROACHES FOR RESOURCE ALLOCATION, NETWORK RESILIENCE, AND DYNAMIC NETWORK ANALYSIS

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Abstract

Graph theory provides a rigorous mathematical language for modelling systems in which resources, agents, infrastructures, information flows, and risks are connected through relational structure. This paper examines graph-theoretic approaches for resource allocation, network resilience, and dynamic network analysis. It argues that graph models are valuable because they convert complex systems into vertices, edges, weights, paths, cuts, layers, and time-indexed structures that can be measured, optimized, simulated, and interpreted. The study follows a descriptive-analytical research design based on author-based secondary literature from network science, combinatorial optimization, resilience theory, multilayer networks, temporal networks, and graph learning. It explains how centrality, matching, network flow, graph cuts, domination logic, spectral indicators, multilayer representations, and temporal graph models support decision-making in engineering, communication systems, logistics, social systems, and infrastructure planning. The paper finds that graph-theoretic tools are strongest when allocation, robustness, and time-dependence are considered together rather than as separate problems. However, practical use is constrained by computational complexity, incomplete data, rapidly changing topology, model uncertainty, and fairness requirements. The paper concludes that future graph-based network analysis should integrate optimization, resilience metrics, dynamic updating, and interpretable algorithms to support adaptive and equitable decision-making in complex networks.

Keywords: graph theory; resource allocation; network resilience; dynamic network analysis; centrality; network flow; temporal networks; multilayer networks; optimization; graph algorithms

1. Introduction

Modern systems rarely operate as isolated units. Communication systems, transport corridors, power grids, supply chains, online platforms, financial dependencies, healthcare referrals, and social organizations all depend on interacting components. Graph theory offers a precise mathematical framework for studying such systems by representing entities as vertices and their relations as edges. The same representation can be used for discrete optimization, resilience assessment, and the study of structural change over time. Newman (2003) argued that complex networks require both structural and functional analysis, while Albert and Barabási (2002) showed that network topology often determines system behaviour more strongly than the properties of individual components. The present paper focuses on three connected problems. The first is resource allocation: how limited resources such as bandwidth, vehicles, energy, personnel, sensors, vaccines, funds, or protective equipment can be assigned across a network. The second is network resilience: how the system responds to node failures, edge removals, overloads, attacks, or cascading disruption. The third is dynamic network analysis: how the graph changes across time and how those changes affect allocation and resilience. Treating these questions separately may produce incomplete decisions. For example, allocating resources only to high-demand nodes can create efficient short-run performance but can also generate fragility if those nodes become overloaded or fail. Similarly, a resilience strategy designed for a static graph may be ineffective when edges appear and disappear over time.

Graph-theoretic approaches are especially important because they translate qualitative system complexity into measurable objects: degree, centrality, connectivity, cuts, paths, components, flows, motifs, spectral properties, temporal paths, and multilayer dependencies. These measurements help identify critical nodes, bottleneck edges, redundant pathways, overloaded communities, vulnerable bridges, and changing patterns of interaction. Such features are used not only in mathematics but also in computer science, operations research, engineering, economics,



epidemiology, and management science.

1.1 Research Problem

The central research problem is that many real-world networks require simultaneous efficiency, robustness, and adaptability. Resource allocation aims to make the best use of scarce capacity, resilience aims to preserve function under disturbance, and dynamic analysis aims to track change. In practice, these objectives often conflict. A highly centralized allocation can be efficient but fragile; a highly redundant network can be robust but expensive; and a dynamic network can invalidate static assumptions. The problem is therefore to examine how graph theory can provide an integrated methodological basis for optimizing resources, measuring resilience, and interpreting network dynamics.

1.2 Objectives of the Study

- To explain the mathematical foundations of graph-theoretic modelling in resource allocation, resilience, and dynamic network analysis.
- To analyse key graph metrics such as degree, centrality, connectivity, cuts, spectral indicators, and temporal reachability.
- To examine how matching, flow, shortest path, cut-set, and community-based methods support resource allocation.
- To evaluate resilience measures under random failure, targeted attack, and cascading disruption.
- To study the role of temporal and multilayer networks in modelling time-dependent and interdependent systems.

2. Review of Literature

The literature on complex networks has expanded from static structural analysis to dynamic, multilayer, and learning-based approaches. Albert and Barabási (2002) provided a foundational account of scale-free networks, growth, and preferential attachment, explaining why hubs frequently emerge in complex systems. Newman (2003) synthesized network structure and function, emphasizing clustering, degree distributions, paths, correlations, and dynamical processes. Boccaletti et al. (2006) extended the discussion to structural dynamics, synchronization, spreading, and control, showing that graph theory is not only descriptive but also predictive.

A second body of literature concerns measurement. Costa et al. (2007) surveyed complex network measures and highlighted the importance of selecting indicators according to the problem being studied. Degree can identify local activity, betweenness can detect brokers and bottlenecks, closeness can measure reachability, and clustering can show local cohesion. Brandes (2008) demonstrated that variants of shortest-path betweenness centrality can be computed generically, making centrality operationally useful for large networks. These studies are relevant because resource allocation and resilience both depend on identifying which vertices and edges carry strategic importance.

A third strand focuses on resilience. Buldyrev et al. (2010) showed that interdependent networks can collapse through cascading failures, even when individual layers appear robust. Matta et al. (2017) proposed vertex attack tolerance as a resilience measure against targeted node removal. Qi et al. (2024) reviewed definitions and approaches to network resilience, noting that resilience is not a single property but a family of concepts that includes robustness, recoverability, adaptability, and functional continuity. These works suggest that resilience analysis must consider not only whether the graph remains connected but also how much function is preserved.

A fourth body of work addresses time and layers. Holme and Saramäki (2012) presented temporal networks as a framework for systems in which edges are activated at different times. Kivela et al. (2014) developed a general theory of multilayer networks, explaining how multiple relationships, layers, and dependencies can be represented in one framework. De Domenico et al. (2015) showed how ranking in multilayer networks can reveal versatile nodes that are important across layers rather than only in one network. More recent research by Longa et al. (2023) and Yang et al. (2023) connects dynamic graphs with graph neural network methods, indicating that graph-theoretic modelling now supports both analytical and learning-based methods.



Table 1. Thematic synthesis of literature used in the study.

Theme	Representative authors	Main contribution	Relevance to this study
Complex network foundations	Albert & Barabási; Newman; Boccaletti et al.	Explains topology, hubs, paths, clustering, and dynamics	Provides the basic model of vertices, edges and structural metrics
Network measurement	Costa et al.; Brandes	Develops metrics for centrality, connectivity and structural characterization	Supports resource prioritisation and bottleneck analysis
Network resilience	Buldyrev et al.; Matta et al.; Qi et al.	Studies robustness, targeted attack and cascading failure	Provides tools to measure system survival under disturbance
Temporal and multilayer networks	Holme & Saramäki; Kivelä et al.; De Domenico et al.	Models evolving and interdependent graphs	Supports dynamic and cross-layer analysis
Graph learning and resource management	Ivanov et al.; Longa et al.; Yang et al.; Singh et al.	Applies graph optimization and learning to changing networked systems	Connects classical graph theory with modern computational applications

3. Research Methodology

This study adopts a descriptive and analytical research design. It is descriptive because it explains the main graph-theoretic concepts, algorithms, metrics, and modelling structures used in resource allocation, network resilience, and dynamic network analysis. It is analytical because it evaluates how these concepts can be combined into an integrated decision framework. The study relies on secondary author-based literature published between 2002 and 2025, including peer-reviewed journal articles, scholarly surveys, books, and mathematical research papers. No government, ministry, state department, or Wikipedia source is used as a reference.

The unit of analysis is a network represented as a graph. A static network is represented by $G = (V, E)$, where V is a set of vertices and E is a set of edges. Weighted graphs include a function $w: E \rightarrow \mathbb{R}$ that assigns capacity, cost, distance, risk, or strength to each edge. Directed graphs represent asymmetric relations. Multilayer networks include several edge types or relational layers. Dynamic networks are represented as a sequence of graphs $G_1, G_2, \dots, G_t$. The paper evaluates methods through conceptual analysis, formula-based modelling, and illustrative figures rather than through a field survey.

Table 2. Methodological framework of the research paper.

Methodological element	Description	Purpose
Research design	Descriptive-analytical review	To explain and evaluate graph-theoretic tools
Data source	Author-based scholarly literature, 2002–2025	To maintain academic and mathematical grounding
Mathematical unit	Graph $G = (V, E)$, weighted, directed, multilayer or temporal	To model resource, resilience and dynamic problems
Analytical tools	Centrality, flow, matching, cuts, spectral and temporal measures	To compare algorithmic and practical relevance
Limitation	No empirical field data or software benchmark	To define the scope as a conceptual mathematical study

4. Mathematical Foundations of Graph-Theoretic Network Modelling



A graph-theoretic model begins by identifying the units of the system and the relationships among them. In a transport network, vertices may be intersections and edges may be roads. In a communication system, vertices may be devices and edges may be links. In a supply network, vertices may be suppliers, warehouses, retailers, and customers. In a social or organizational network, vertices may be people, teams, or institutions. Once a network is represented as a graph, mathematical tools can be used to evaluate reachability, redundancy, centrality, capacity, and vulnerability.

$$G = (V, E), |V| = n, |E| = m$$

Basic graph representation, where V is the set of vertices and E is the set of edges.

$$A = [a_{ij}], \quad a_{ij} = 1 \text{ if } (v_i, v_j) \in E, \text{ and } 0 \text{ otherwise}$$

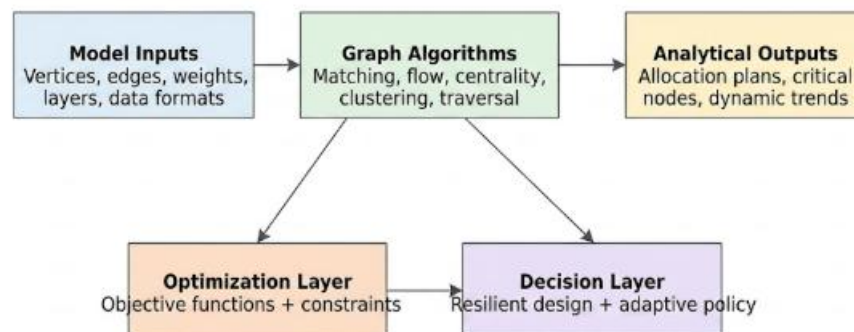
Adjacency matrix representation of an unweighted graph.

The adjacency matrix is especially useful for computational analysis. Matrix powers can indicate walks of different lengths, while eigenvalues and eigenvectors can reveal structural features. Weighted adjacency matrices are used when edges have capacities, costs, distances, frequencies, delays, or risks. In resource allocation, the weights can represent available capacity or allocation cost. In resilience analysis, weights may represent vulnerability, dependency strength, or recovery time.

Table 3. Key graph measures and formulas.

Measure	Formula	Interpretation	Use in this paper
Degree centrality	$C_D(v) = \deg(v)/(n - 1)$	Local connectivity of vertex v	Identifies active or exposed vertices
Betweenness centrality	$C_B(v) = \sum \sigma_{st}(v)/\sigma_{st}$	Control over shortest paths	Detects brokers, bottlenecks and critical nodes
Closeness centrality	$C_C(v) = (n-1)/\sum d(v,u)$	Average reachability	Helps allocate mobile or emergency resources
Edge cut	$\delta(S) = \{(u,v): u \in S, v \notin S\}$	Boundary between vertex subsets	Locates vulnerability and separation points
Resilience ratio	$R(q) = S(q)/S(0)$	Remaining functional component after removals	Measures robustness under disturbance
Dynamic change	$\Delta A_t = A_t - A_{\{t-1\}}$	Change in graph structure over time	Tracks evolving networks

Figure 1. Conceptual framework for graph-theoretic network analysis.



5. Graph-Theoretic Approaches for Resource Allocation

Resource allocation problems ask how a limited resource should be distributed over a graph. In a network, a resource



may be material, computational, financial, informational, or human. Graph theory makes allocation problems precise by defining objectives and constraints. A matching model allocates resources by pairing vertices. A flow model allocates capacity from sources to sinks. A coloring model separates conflicting users or channels. A domination model identifies a small set of vertices that can cover or influence the rest of the graph. A facility-location model places services near demand nodes.

Ivanov et al. (2022) show that graph-based resource allocation is useful in communication networks because interference, routing, channel allocation, and coverage can be represented through graph structure. In mathematics, the same logic applies to many allocation tasks. A bipartite graph can match tasks to workers, resources to users, or clients to facilities. A weighted graph can find minimum-cost routes or maximum-capacity paths. A conflict graph can ensure that incompatible users do not share the same channel or resource.

$$\text{minimize } \sum_{e \in E} c_e x_e \quad \text{subject to } Bx = b, 0 \leq x_e \leq u_e$$

Generic network-flow allocation model with cost c_e , incidence matrix B , demand vector b , and capacity u_e .

$$\text{Maximize } U(x) = \sum_i u_i(x_i) \quad \text{subject to } \sum_i x_i \leq C, x_i \geq 0$$

Utility-based allocation model under total capacity C .

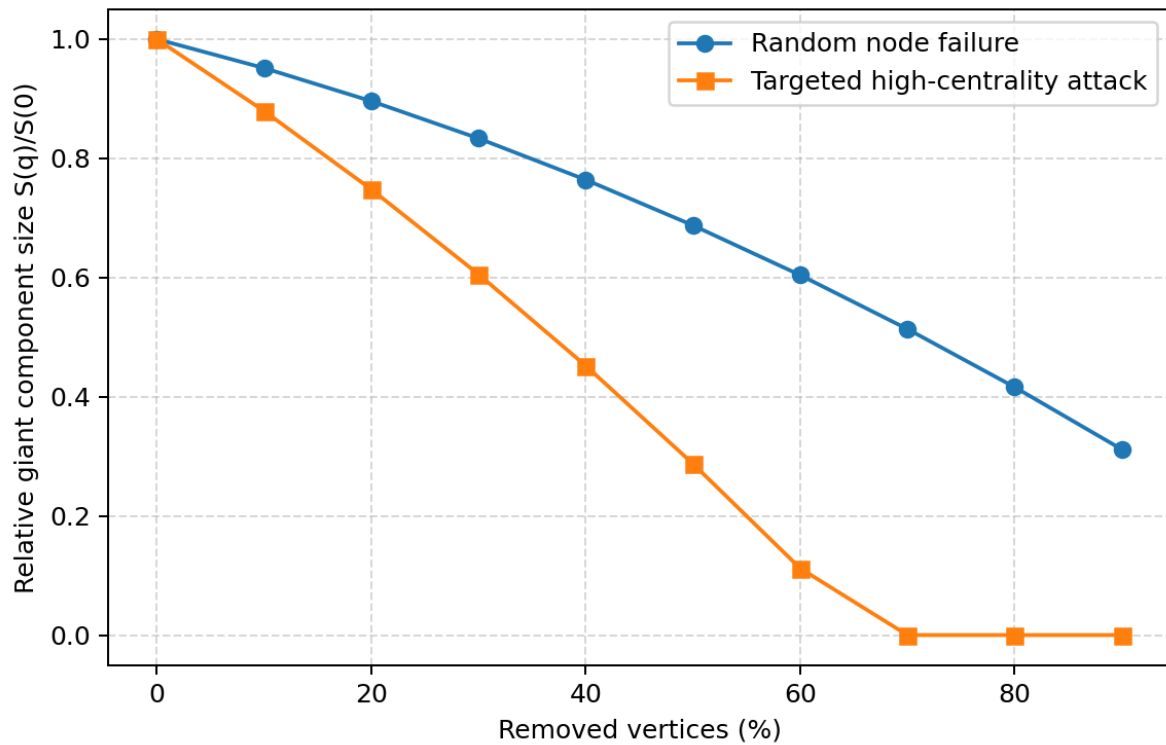
The first model is suitable when allocation is represented by flows on edges. The second model is suitable when a fixed quantity of resource must be divided among vertices or agents. In graph-theoretic decision-making, the important point is not only the size of the allocation but also where in the graph it occurs. Allocating extra capacity to a peripheral vertex may benefit a local region, while allocating to a high-betweenness vertex may improve system-wide throughput. However, excessive reliance on central vertices can create vulnerability, which is why allocation should be linked to resilience.

Table 4. Algorithmic tools for graph-based resource allocation.

Problem type	Graph model	Typical algorithm	Indicative complexity	Decision use
Shortest routing	Weighted graph	Dijkstra or Bellman-Ford variants	$O(m \log n)$ in common implementations	Finds low-cost paths
Maximum flow	Capacitated directed graph	Ford-Fulkerson / Edmonds-Karp / Dinic	Depends on implementation and capacity model	Allocates capacity from sources to sinks
Assignment	Bipartite graph	Hungarian or matching algorithms	Polynomial time	Matches tasks and resources
Conflict allocation	Conflict graph	Graph coloring heuristics	NP-hard in general	Separates incompatible allocations
Facility coverage	Dominating set or p-median model	Exact ILP or approximation heuristics	NP-hard in general	Places services or monitors
Adaptive allocation	Temporal or dynamic graph	Rolling optimization or graph learning	High, data-dependent	Updates decisions as the network changes

Figure 2. Example of centrality-guided resource prioritisation.





7. Dynamic Network Analysis

Dynamic network analysis studies networks whose vertex set, edge set, edge weights, or attributes change over time. Traditional graph theory often starts with a static graph, but many real systems are temporal. Roads may become congested during peak hours, communication links may fail temporarily, financial exposures change daily, and social interactions are episodic. Holme and Saramäki (2012) argue that time cannot always be treated as a secondary attribute because the order of interactions may determine whether information, disease, or resources can move through the network.

$$\mathcal{G} = \{G_1, G_2, \dots, G_T\}, \text{ where } G_t = (V_t, E_t, w_t)$$

A dynamic graph represented as a time-indexed sequence of graph snapshots.

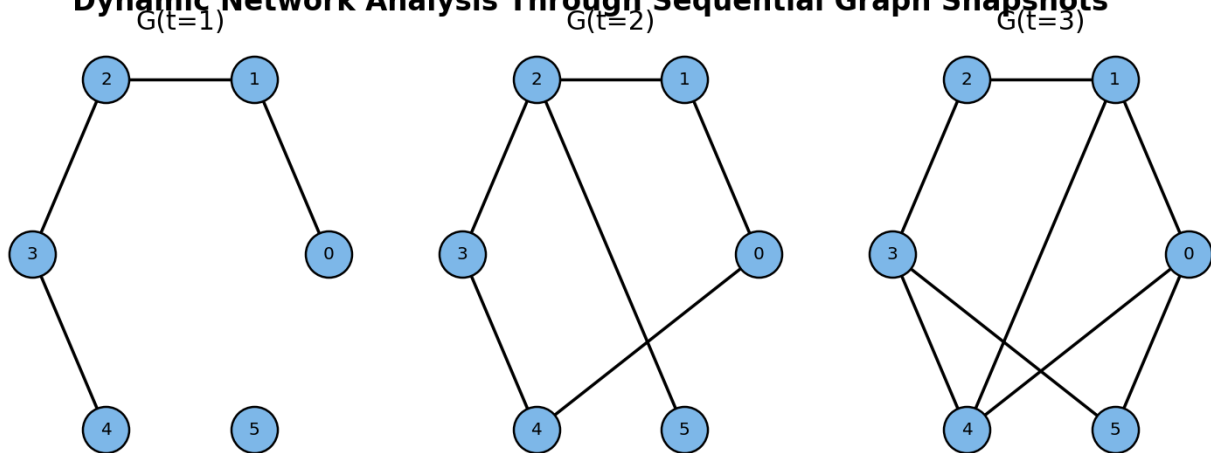
$$\Delta A_t = A_t - A_{t-1}$$

Change in the adjacency matrix between two consecutive time points.

Dynamic analysis enables three important tasks. First, it identifies structural change, such as new bridges, disappearing links, or growing communities. Second, it predicts future network states, such as link formation or capacity pressure. Third, it supports adaptive allocation by updating decisions when graph structure changes. Longa et al. (2023) and Yang et al. (2023) show that temporal graph learning has become a major research direction because static graph models cannot fully represent systems in which topology and attributes evolve together.

Figure 4. Dynamic network analysis through sequential graph snapshots.

Dynamic Network Analysis Through Sequential Graph Snapshots



8. Multilayer Networks and Interdependent Systems

Many networks are not single-layer structures. A city may have road, rail, electricity, water, and communication layers. A business network may have supply, finance, information, and trust layers. A social system may include family, work, digital, and institutional relations. Kivelä et al. (2014) show that multilayer networks provide a formal language for representing systems with multiple kinds of relations. De Domenico et al. (2015) argue that rankings in multilayer networks can identify versatile nodes, meaning nodes whose importance comes from activity across layers rather than dominance in only one layer.

In a multilayer graph, a vertex may have different roles in different layers. A node can be peripheral in a transport layer but central in an information layer. This matters for resource allocation because resource decisions made in one layer may affect another layer. It also matters for resilience because a failure in one layer may propagate through dependency edges. For this reason, multilayer analysis is essential for infrastructure systems, socio-technical systems, and digital platforms.

$$M = (V, L, E_{\text{intra}}, E_{\text{inter}})$$

Multilayer network with vertices V , layers L , intra-layer edges and inter-layer dependency edges.

$$C_{\text{multi}}(v) = \sum_{\ell \in L} \alpha_{\ell} C_{\ell}(v)$$

Layer-weighted centrality of vertex v across layers, where α_{ℓ} represents the importance of layer ℓ .

The layer-weighted centrality formula is useful when a decision-maker wants a single importance score while still respecting layer differences. If the transport layer is more important than the communication layer for a specific application, its weight can be increased. If resilience is the goal, weights may reflect failure consequences rather than traffic volume. This flexibility makes multilayer graph theory useful in planning problems where priorities vary across contexts.

9. Integrated Framework: Allocation, Resilience and Dynamics

An integrated graph-theoretic approach treats allocation, resilience, and dynamic analysis as mutually connected. A resource allocation plan should not only maximize efficiency but also avoid creating fragile concentration. A resilience plan should not only add redundancy but also consider cost and capacity. Dynamic analysis should not only describe change but also update allocation and resilience policies as the graph evolves. The integrated framework proposed here uses four steps: model construction, metric calculation, optimization, and adaptive monitoring.

In the model construction stage, the researcher defines vertices, edges, weights, layers, and time steps. In the metric stage, the researcher calculates centrality, connectivity, cuts, components, and temporal indicators. In the optimization stage, resources are assigned according to objectives and constraints. In the adaptive monitoring stage,

the graph is updated and the allocation is revised. This cycle allows decision-makers to move from static planning toward adaptive network governance.

$$\text{Score}(v,t) = \beta_1 C_B(v,t) + \beta_2 C_D(v,t) + \beta_3 \text{Risk}(v,t) - \beta_4 \text{Redundancy}(v,t)$$

Example priority score for deciding where to place resources or protective capacity at time t .

The above score is not a universal formula; it is a flexible decision model. Betweenness and degree can increase priority because they indicate importance. Risk can increase priority because vulnerable nodes need protection. Redundancy can reduce priority because alternative paths already exist. The coefficients β_1 , β_2 , β_3 , and β_4 can be chosen according to the application. In emergency logistics, risk may receive a high weight. In data routing, betweenness and capacity may receive higher weights. In social service allocation, fairness constraints may be added.

10. Algorithmic Complexity and Computational Considerations

Graph-theoretic methods vary substantially in computational cost. Breadth-first search, connected components, and simple degree measures are comparatively inexpensive. Shortest path and centrality computations become more demanding on large graphs. Exact formulations of coloring, domination, facility location, and many cut problems can become NP-hard. Dynamic and multilayer graphs increase complexity because the number of vertices and edges may be multiplied by layers and time steps. This creates a trade-off between model realism and computational tractability.

Complexity matters because networked systems may contain thousands or millions of vertices. In such cases, exact optimization may be replaced by heuristics, approximation algorithms, sampling, decomposition, or learning-based models. Graph neural networks and temporal graph models have become increasingly important because they can learn structural patterns from data, but they also raise interpretability and generalization concerns. The practical challenge is to choose a method that is mathematically defensible and computationally feasible.

Figure 5. Relative complexity of selected graph-theoretic tools.

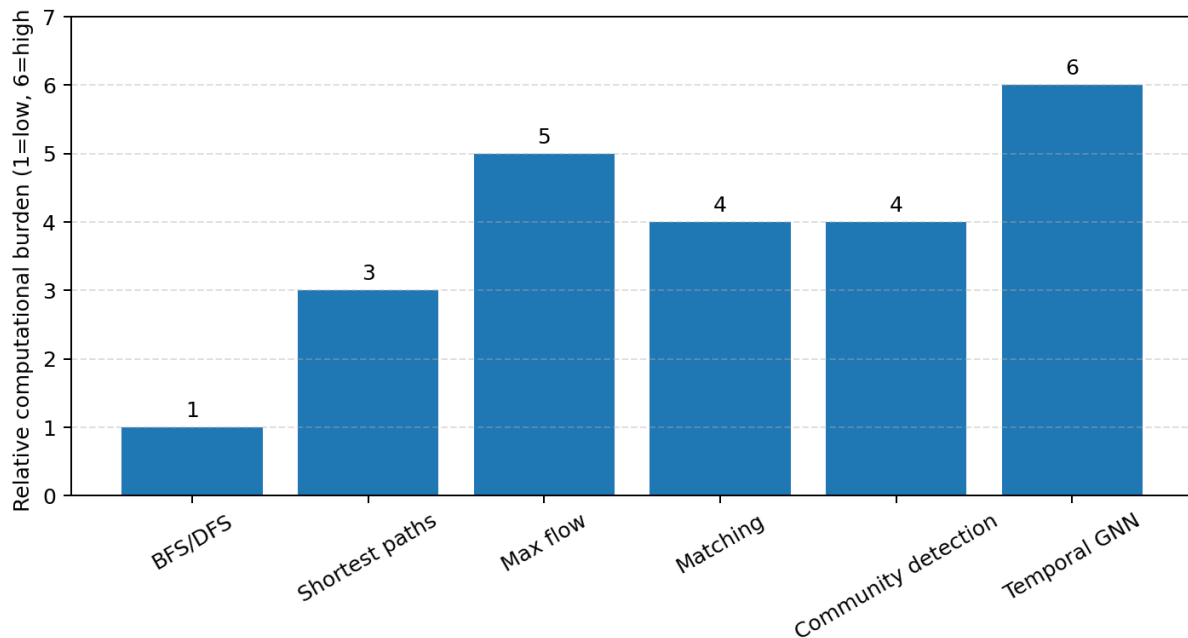


Table 5. Applications of graph-theoretic approaches.

Application area	Graph representation	Typical method	Main benefit	Risk/limitation
Communication networks	Devices and links with bandwidth or interference weights	Flow, coloring, graph learning	Efficient spectrum and capacity allocation	Rapid topology change and data load



Transportation and logistics	Locations as vertices, routes as weighted edges	Shortest path, flow, facility location	Better routing and service placement	Congestion and disruptions change edge weights
Infrastructure resilience	Interdependent physical and control systems	Cuts, percolation, cascade simulation	Identification of vulnerable nodes and bridges	Dependency data may be incomplete
Supply chains	Firms, warehouses and demand nodes	Multilayer and flow models	Allocation under capacity and disruption constraints	Multi-tier dependencies are hard to observe
Public services	Communities, facilities and mobility links	Coverage, domination and centrality	Equitable placement of limited resources	Fairness cannot be reduced to topology alone
Digital platforms	Users, content and interaction layers	Dynamic graphs and temporal learning	Prediction of changing engagement patterns	Privacy, bias and explainability challenges

11. Data Interpretation and Findings

The analysis produces five major findings. First, graph theory is a unifying mathematical framework because it can represent allocation, risk, and change within the same formal structure. A network-flow model, a centrality model, and a temporal snapshot model may appear different, but each is built on vertices, edges, weights, and relations. Second, resource allocation decisions are improved when topological importance is considered. A vertex with high betweenness may need capacity support because it controls many paths; a vertex with low degree but high local demand may need local resource support. Therefore, allocation should combine graph metrics with contextual priorities.

Third, resilience is not equivalent to connectivity alone. A graph may remain connected but lose major capacity or service function. Resilience measures should include component size, path length, flow capacity, recovery time, redundancy, and functional output. Fourth, dynamic network analysis is essential for systems in which interaction patterns change over time. A static graph can hide temporal bottlenecks or overestimate reachability. Fifth, algorithmic complexity requires careful method selection. Simple metrics are interpretable but may be insufficient; exact optimization is rigorous but may be computationally difficult; graph learning is powerful but can be less transparent.

Table 6. Summary of findings.

Finding	Explanation	Implication
Topology matters	Network position affects allocation outcomes	Use centrality and connectivity before distributing resources
Efficiency can create fragility	Centralized allocations may overload hubs	Combine efficiency metrics with resilience checks
Resilience is multidimensional	Connectivity, flow and recovery are different properties	Use multiple measures rather than a single indicator
Time changes conclusions	Paths and centrality can shift across snapshots	Use dynamic graphs when interactions are time-dependent
Complexity limits exact methods	Many useful problems are NP-hard or data-intensive	Use heuristics, decomposition and interpretable approximation

12. Recommendations



- Use graph modelling at the earliest stage of network planning so that allocation decisions are based on structure rather than only aggregate demand.
- Apply at least two complementary metrics: one for efficiency, such as shortest path or flow, and one for vulnerability, such as cut size or resilience ratio.
- Avoid overdependence on high-centrality hubs; if hubs receive more resources, they should also receive redundancy and protection.
- Use multilayer modelling when systems include physical, digital, social or administrative dependencies across different relational layers.
- Use dynamic graph snapshots or temporal graphs when network conditions vary by time, event, demand cycle or disruption state.
- Combine exact optimization with heuristics for large networks, because exact methods may be computationally impractical in real-time settings.
- Include fairness and service-access constraints when graph theory is applied to public resource allocation, since mathematical efficiency alone may not produce equitable outcomes.
- Maintain interpretability when using graph learning, especially in high-stakes domains such as infrastructure resilience, public services and emergency response.

13. Conclusion

Graph-theoretic approaches provide a powerful mathematical basis for analysing resource allocation, network resilience, and dynamic network behaviour. Their strength lies in the ability to convert complex relationships into formal structures that can be measured, optimized, simulated and updated. The paper has shown that resource allocation can be formulated through matching, flow, coloring, domination, and facility-location models. It has also shown that resilience can be studied through component preservation, cut sets, robustness curves, attack tolerance, and cascade analysis. Dynamic network analysis extends these tools by recognising that networks evolve across time and that temporal order influences reachability and performance.

The central conclusion is that allocation, resilience, and dynamics should be treated as an integrated graph-theoretic problem. Efficient allocation without resilience may create fragile networks; resilience without optimization may be costly; and static modelling without dynamic updating may misrepresent reality. A strong graph-theoretic framework therefore needs mathematical clarity, computational feasibility, resilience awareness, temporal sensitivity, and ethical attention to fairness. Future research should develop interpretable algorithms that can operate on large multilayer temporal graphs while balancing efficiency, robustness and equitable resource distribution.

Appendix A. Illustrative Graph-Analysis Workflow

The following workflow may be used when a researcher applies graph theory to a real networked problem. First, define the graph boundary and decide whether the model is static, weighted, directed, multilayer, or temporal. Second, collect or construct the edge list and verify whether missing edges may distort the analysis. Third, compute basic structural indicators such as degree distribution, components, average path length, clustering and centrality. Fourth, formulate the allocation or resilience objective in mathematical form. Fifth, run the appropriate algorithm and compare the result under at least two scenarios: normal operation and disturbed operation. Sixth, interpret the result cautiously by connecting mathematical output with domain knowledge.

Table 7. Practical workflow for graph-theoretic network analysis.

Step	Operation	Mathematical object	Output
1	Define system boundary	V, E and attributes	Valid graph scope
2	Construct network	Edge list or adjacency matrix A	Computable graph model
3	Measure structure	C_D, C_B, components, cuts	Critical vertices and weak points
4	Formulate objective	min/max function with constraints	Optimization problem



5	Test disturbance	R(q), attacks, failures, time snapshots	Resilience profile
6	Revise decision	Updated G_t and new parameters	Adaptive allocation strategy

This workflow shows that graph theory is not merely a visualization technique. It is a mathematical decision process that begins with modelling assumptions and ends with interpretable, scenario-tested recommendations.

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